Abstract

Machine learning usually assumes that attribute values, as well as class labels, are either known precisely or not known at all. However, in our attempt to automate evaluation of intrusion detection systems, we have encountered ambiguous examples such that, for instance, an attribute’s value in a given example is known to be a or b but definitely not c or d. Previous research usually either “disambiguated” the value by giving preference to a or b, or just replaced it with a “don’t-know” symbol. Disliking both of these two approaches, we decided to explore the behavior of other ways to address the situation. To keep the work focused, we limited ourselves to nearest-neighbor classifiers. The paper describes a few techniques and reports relevant experiments. We also discuss certain ambiguity-related issues that deserve closer attention.

Introduction

The common assumption in concept learning is that all attribute values are either established precisely or totally unknown. In some domains, though, the expert who prepares the data may know some attributes only to a certain extent. We have encountered this problem when seeking to evaluate the performance of an intrusion detection system (IDS), a software package capable of classifying specific events in a computer network. Table 1 illustrates our training set by three (simplified) examples, each described by such attributes as protocol, event, or operating-system, and by the type of attack, if any, indicated by the IDS. The class label specifies whether the IDS’s “opinion” about the event was correct and, if not, what type of error was made. Thus in the first example, the operating system is only known to be either WinXP or Win2k3 and that the class label is either correct or false-positive. We need a technique capable of handling data ambiguities of this kind. If only one attribute were ambiguous, then we could perhaps consider the possibility to split it into two or more examples, one for each option. This is impracticable in a situation where several attributes are ambiguous and one would have to create a separate new example for each combination of alternative values.

Table 1: Three training examples from the IDS Domain. Some attribute values are ambiguous.

<table>
<thead>
<tr>
<th>Case</th>
<th>Protocol</th>
<th>Event</th>
<th>OS</th>
<th>Attack Type</th>
<th>CLASS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>UDP</td>
<td>App. Alter</td>
<td>WinXP</td>
<td>Exploit</td>
<td>False Pos. Correct</td>
</tr>
<tr>
<td>2</td>
<td>ICMP</td>
<td>App. Alter</td>
<td>Linux</td>
<td>DSS</td>
<td>False Neg.</td>
</tr>
<tr>
<td>3</td>
<td>TCP</td>
<td>Web</td>
<td>Win2k3</td>
<td>Recon.</td>
<td></td>
</tr>
</tbody>
</table>

The field of uncertainty processing has studied similar problems for decades but the machine learning community, with a few laudable exceptions, has failed to pay adequate attention to them. Thus (Denoeux and Skarstein) and (Elouedi, Mellouli, and K. Smets) have modified the algorithm for decision-tree induction using the Dempster-Shafer theory of evidence, and as for instance-based classifiers, class label ambiguities (but not attribute-value ambiguities) have been considered by (Denoeux) that, too, relied on the Dempster-Shafer theory. Unfortunately, all these authors just offered theoretical solutions without supporting them with systematic experiments. And yet, we believe that our network intrusion domain is hardly the only one of this kind—similar features characterize, for instance, the “Lebowitz’s Universities Database” from the UCI repository (Newman, Hettich, and Merz). This is why we decided to take a closer look.

It is more than likely that any machine-learning paradigm (decision trees, bayesian classifiers, etc.) may call for different measures. To start with, we focused on the nearest neighbor classifiers (k-NN). In the work reported here, we first established that data ambiguities indeed compromise classification performance. Therefore, we suggested alternative ways to modify the k-NN classifier accordingly: we re-defined the notion of vector-to-vector similarity, and then proposed a mechanism to choose class labels from the ambiguous labels found in the k neighbors. Finally, to learn more about how classification results might be affected by different degrees of ambiguity, we (1) modified the notion of classification performance, then (2) found a way to quantify the ambiguities in the data and then (3) experimented not only with our own data, but also with domains where the amount of these ambiguities can be controlled.
Problem Statement

The learner’s input consists of training examples, \([x, C(x)]\), such that \(x = (x_1, x_2, \ldots, x_M)\) describes the example by discrete attributes and \(C(x)\) is the class label. We assume that any attribute, and any class label, can be ambiguous—for instance, \(x_i = [a, b]\) is interpreted as meaning that the value of \(x_i\) is either \(a\) or \(b\) (but no other value). The task is to induce a classifier that will determine the class labels of future examples. When evaluating its performance, we have to keep in mind that the testing examples, too, can be ambiguously described. This has to be reflected in the employed performance criterion—if a testing example’s class is known to be either \(C_1\) or \(C_2\), then a classifier that predicts \(C_1\) should be deemed less accurate than one that predicts \([C_1, C_2]\).

Let \(N\) be the number of testing examples, let \(C_{i,\text{known}}\) be the set of class labels of the \(i\)-th testing example, and let \(C_{i,\text{classified}}\) be the set of class labels given to the \(i\)-th testing example by the classifier. We evaluate the classification performance of this classifier by the following formula:

\[
\text{AmbA} = \frac{1}{N} \sum_{i=1}^{N} \text{Acc}_i; \quad \text{where} \quad \text{Acc}_i = \frac{|C_{i,\text{known}} \cap C_{i,\text{classified}}|}{|C_{i,\text{known}} \cup C_{i,\text{classified}}|}
\]

Furthermore, we need a mechanism to quantify the amount of ambiguity in the data. Suppose that, in a given example, an attribute is given \(n_A\) out of \(n_T\) of different values. For instance, if the attribute can acquire values \([a, b, c, d, e]\) and is known to be either \(a\) or \(b\), for the given example, then \(n_T = 5\) and \(n_A = 2\). The amount of ambiguity is then quantified as follows:

\[
AAmb = \frac{n_A - 1}{n_T - 1}
\]

This ensures that \(AAmb = 0\) if the value is known precisely \((n_A - 1 = 0)\) and \(AAmb = 1\) if the value is totally unknown. Note that each attribute must be able to acquire at least two different values so that \(n_T > 1\). The total amount of attribute-value ambiguity in the data can be assessed either by taking the average value of \(AAmb\) over all example-attribute pairs or over only those example-attribute pairs where the attribute value is ambiguous. In the following formula, \(m\) is the number of example-attribute pairs considered.

\[
AAmb_{\text{total}} = \frac{1}{m} \sum_{j} \frac{n_A(j) - 1}{n_T(j) - 1} \times 100\%
\]

Handling Ambiguity in k-NN Classifiers

Let us first discuss how to handle the voting mechanism, and then turn our attention to the assessment of example-to-example similarity.

### Table 2: Ambiguous class labels from a k-NN classifier

<table>
<thead>
<tr>
<th>Class Labels</th>
<th>Nearest Neighbor 1</th>
<th>Nearest Neighbor 2</th>
<th>Nearest Neighbor 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>(C_1) or (C_2)</td>
<td>(C_1) or (C_3) or (C_4)</td>
<td>(C_2)</td>
<td></td>
</tr>
</tbody>
</table>

### Table 3: Voting about the class label based on the nearest neighbors listed in Table 2

<table>
<thead>
<tr>
<th>(W_{\text{factor}}(C))</th>
<th>(C_1)</th>
<th>(C_2)</th>
<th>(C_3)</th>
<th>(C_4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\theta = \frac{3}{4})</td>
<td>(\frac{2}{3} + \frac{1}{3})</td>
<td>(\frac{1}{2})</td>
<td>(\frac{1}{3} + \frac{2}{3})</td>
<td>(\frac{1}{4} + \frac{3}{4})</td>
</tr>
</tbody>
</table>

Voting Mechanism

In the example from Table 2, the 3-NN classifier has already identified the three nearest neighbors, some of which have more than one class label (because the true class is known only partially). Labeling the testing example with a union of these labels would not reflect the different degree of “focus” in the individual neighbors. Thus the fact that the first neighbor suggests classes \([C_1, C_2]\) and the third neighbor suggests only \(C_2\) seems to indicate we should have more confidence in the latter.

This is why we weigh each label by the focus of the given example. Let \(N_{i,c} = 1\) if class \(c\) is found among the labels of the \(i\)-th nearest neighbor and let \(N_{i,c} = 0\) if it is not. If \(N_{i,\text{total}}\) is the number of labels in the \(i\)-th nearest neighbor, then, for \(k\) nearest neighbors, we calculate the weight of class \(c\) as follows:

\[
W_{\text{factor}}(C) = \frac{1}{k} \sum_{i=1}^{k} N_{i,c} \frac{N_{i,c}}{N_{i,\text{total}}}
\]

For the case of the three nearest neighbors from Table 2, the class weights are calculated in Table 3. The system chooses classes whose weights exceed a user’s threshold, \(\theta\). For instance, if \(\theta = 0.4\), class \(C_2\) is chosen; if \(\theta = 0.2\), classes \([C_1, C_2]\) are chosen.

Example-to-Example Similarity

Suppose that \(x = (x_1, \ldots, x_M)\) and \(y = (y_1, \ldots, y_M)\) are examples. Nearest-neighbor classifiers usually calculate the similarity of these \(x\) and \(y\) from the similarity along the individual attributes:

\[
S(x, y) = \sum_{i=1}^{n} s(x_i, y_i)
\]

In our context, \(s(x_i, y_i)\) has to reflect the ambiguities in \(x_i\) and \(y_i\). Let us show three simple ways on how to handle the problem in traditional \(k\)-NN classifiers, and then proceed to our own solution.
Traditional Nearest Neighbor Approaches. Classical k-NN classifiers usually assume that each attribute is either known precisely or totally unknown (replaced with a question mark). In our experiments, we used the following three alternatives.

\( k-\text{NNa:} \) If \( x_i = y_i \), then \( s(x_i, y_i) = 0 \); if \( x_i \neq y_i \), then \( s(x_i, y_i) = 1 \); and if a question mark is encountered in either \( x_i \) or \( y_i \), then \( s(x_i, y_i) = 1 \). These values are then summed over all \( M \) attributes:

\[
S(x, y) = \sum_{i=1}^{M} s(x_i, y_i); \quad \text{where}
\]

\[
s(x_i, y_i) = \begin{cases} 
1 & y_i \neq x_i \\
0 & y_i = x_i \\
1 & ? \text{ or } x_i = ?
\end{cases}
\]

\( k-\text{NNb:} \) If the ambiguities are rare, we can afford ignoring the unknown attribute values altogether. For all the remaining attributes, \( x_i = y_i \) implies \( s(x_i, y_i) = 0 \) and \( x_i \neq y_i \) implies \( s(x_i, y_i) = 1 \). Denoting by \( M_1 \) the number of unambiguous attributes, we use the following formula:

\[
S(x, y) = \sum_{i=1}^{M_1} s(x_i, y_i); \quad \text{where}
\]

\[
s(x_i, y_i) = \begin{cases} 
1 & y_i \neq x_i \\
0 & y_i = x_i
\end{cases}
\]

\( k-\text{NNc:} \) Yet another possibility is to replace each question mark with the most frequent value of the given attribute. The similarity-calculating formula then remains unchanged:

\[
S(x, y) = \sum_{i=1}^{M} s(x_i, y_i); \quad \text{where}
\]

\[
s(x_i, y_i) = \begin{cases} 
1 & y_i \neq x_i \\
0 & y_i = x_i
\end{cases}
\]

Ambiguous Nearest Neighbor Approach: \( k-\text{AmbNN} \). More complicated is the case where the training set gives, for the given example-attribute pair, a proper subset of possible values. Let us denote by \( x_i \) and \( y_i \) the sets of values of the \( i \)-th attribute in \( x \) and \( y \). To make sure that the similarity between \( x \) and \( y \) reflects the relation between the sets \( x_i \) and \( y_i \), we use the following formula.

\[
S(x, y)_{k-\text{AmbNN}} = \sum_{i=1}^{n} \frac{|x_i \cap y_i|}{|x_i| + |y_i|}
\]

Note that the formula degenerates into the “traditional” approach where at least one of the values is replaced with a “?” (see above).

For illustration, consider a simple domain where the examples are described by \text{season} (SPRING, SUMMER, FALL, WINTER) air quality (DRY, HUMID), and \text{day-time} (DAY, NIGHT). The similarity of the two examples from Table 4 is obtained as follows:

\[
S(x, y)_{k-\text{AmbNN}} = \frac{|\text{SPRING} \cap \text{DAY}|}{|\text{SPRING}| + |\text{DAY}|} + \frac{|\text{DRY} \cap \text{DAY}|}{|\text{DRY}| + |\text{DAY}|} = \frac{1}{3} + \frac{1}{3} = 1.5
\]

Fuzzy Nearest Neighbor: \( k\text{-fuzzyNN} \)

For the sake of comparison with some earlier work in uncertainty processing, we also implemented a fuzzy voting mechanism. The idea is to consider the degree of membership of the training example in a class. We use the following definitions:

- \( n_c \) ... number of classes,
- \( k \) ... number of nearest neighbors,
- \( 1 \leq j \leq k \) ... \( j \)-th neighbor,
- \( \mu_i(y_j) \) ... membership of the neighbor, \( y_j \), in the \( i \)-th class,
- \( \mu_i(x) \) ... membership of the training example, \( x \), in the \( i \)-th class,
- \( ||x - y_j|| \) ... the distance between \( x \) and \( y_j \)
- \( 1.0 \leq w \leq 2.0 \) ... a fuzzy parameter

The following formula, based on ideas developed by (Keller), represents the normalized membership for each of the class labels.

\[
\mu_i(x) = \frac{\sum_{j=1}^{k} \mu_i(y_j) \cdot (||x - y_j||^{-w})}{\sum_{k=1}^{k} (||x - y_j||^{-w})}, \quad i = 1, 2, \ldots, n_c
\]

Note that we are using distance \( ||x - y_j|| \) instead of similarity. Furthermore, note that the formula involves two parameters: \( w \) and \( b_{\text{fuzzy}} \), the latter being a threshold that controls the class selection.

Experimental Data

Primarily, we wanted to apply our algorithms to the domain that has inspired this research—intrusion detection. Then, to learn more about the behavior of the individual formulas, we also used one domain from the UCI repository and one synthetic domain.

Network Intrusion Detection System Data

The data file was compiled from observations made on a concrete computer network as a result of a number of measurements. The collected data included the protocol of the incoming network request, the event that took place due to the request, analyzed attack type, type of operating system.
targeted in the attack, system used for intrusion detection, and possible classification labels: False Positive, False Negative, and Correctly classified.

Table 5 summarizes attributes that acquire ambiguous values. The ambiguity is due to the network administrator’s limited ability to interpret the corresponding log files. Other attributes were unambiguous—in reality, there were 10 attributes and 126 examples. The amount of ambiguity according to Equation 4 is 30%.

**UCI Domain**

The Lebowitz’s universities domain was compiled in July 1988 and consists of 285 instances (including duplicates) with 17 attributes. One of the attributes(academic-emphasis) acquires ambiguous values, other attributes have missing values. We eliminated duplicate examples.

**Synthetic Domains**

Maximum experimental flexibility is provided only by synthetic domains that allow the researcher freely to adjust data parameters. The one we used in this research was created with the help of decision trees. First, we randomly generated artificial examples described by 10 multi-valued discrete attributes. Then, we manually created the decision tree shown in Figure 1 and truncated it, obtaining the tree in Figure 2 that was then used to classify the data. Note that some of the leaves contain more than one class—this introduces the class-label ambiguity. Attribute ambiguity is introduced by randomly selecting an attribute and adding the most frequently occurring value to it. The amount of ambiguity is controlled by the parameter $AAmb$ defined earlier—in alternative versions of the data, $AAmb$ ranged from 10% to 50%.

**Experimental Results**

First, we wanted to learn how the performance is affected by the cut-off point, $\theta$, used in the voting mechanism—recall that the testing example is assigned all class labels for which $W_{factor}(c) > \theta$. High values of $\theta$ lead to the “crisp” single-label case, or even to the situation where no class label exceeds $\theta$. Conversely, very low values will render the labeling more ambiguous than necessary. We measured the classification performance by the $AAmb$ metric defined by Equation 1. For the synthetic data, Table 6 shows the values of $AAmb$ for different values of $\theta$. The results indicate that the optimum cut-off is somewhere between 0.3 and 0.5, and that its optimum value depends also on the number, $k$, of the nearest neighbors employed.

In the experiments reported in the rest of this section, we always used $\theta = 0.3$ while understanding that the fine-tuning of $\theta$ to the specific needs of a concrete domain might further improve the results. Further on, the reader is reminded that, for ambiguous domains, we have defined a performance metric, $AAmb$, whose behavior is different from the classical classification accuracy. If a testing example belongs to classes $(C_1, C_2)$ and the classifier outputs $(\hat{C}_2)$, then $Acc = 0.5$. Note that the values of $AAmb$ are typically lower than those of the classification accuracy.

For the fuzzy nearest neighbor approach ($k$-fuzzyNN), established (by experiments not reported here) that the best choice of the parameter $w$ was—at least for the domains we worked with—$w = 2.0$.

Figure 3 compares the performance of $k$-AmbNN with

Table 6: AmbA-performance for different cut-off points and $k$-values as evaluated on synthetic domain with $AAmb = 30\%$.

<table>
<thead>
<tr>
<th>$k$</th>
<th>0.1</th>
<th>0.2</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.8</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
<td>0.385</td>
</tr>
<tr>
<td>3</td>
<td>0.285</td>
<td>0.285</td>
<td>0.366</td>
<td>0.366</td>
<td>0.366</td>
<td>0.112</td>
<td>0.112</td>
<td>0</td>
</tr>
<tr>
<td>5</td>
<td>0.416</td>
<td>0.416</td>
<td>0.416</td>
<td>0.416</td>
<td>0.248</td>
<td>0.019</td>
<td>0.019</td>
<td>0</td>
</tr>
<tr>
<td>9</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
</tr>
</tbody>
</table>

Footnote: Sample domains can be downloaded from http://umsis.miami.edu/~hholland/k-ANN/. For additional support, please contact Hans Holland (hholland@miami.edu)
that of $k$-NN and $k$-fuzzyNN in the intrusion detection domain for different values of $k$. To be able to use $k$-NN, we replaced ambiguous values with question marks. The individual points in the charts have been obtained as averages from the 5x2 cross-validation, a methodology recommended for the assessment of machine learning algorithms by (Dietterich). The reader can see that $k$-AmbNN consistently outperforms the other approaches over a whole range of $k$-values. Since $k$-NN systematically underperforms $k$-AmbNN, we conclude that replacing partial ambiguity with total ambiguity is indeed unnecessary and harmful. Interestingly, whereas $k$-NN's performance dropped with the growing value of $k$ (perhaps due to the sparseness of the data), $k$-AmbNN's performance grew with increasing $k$. The margin between $k$-NN and $k$-AmbNN is statistically significant according to the two-tailed t-test with a confidence level of 2%. The fuzzy approach does not seem to be appropriate, here. We surmise that our ambiguities are too simple for the fuzzy-set approach to fully unfold its strength.

Figure 4 corroborates all these observations by experiments with the university domain. In this sparser, but less noisy domain, even $k$-AmbNN's performance tended to drop with growing $k$, although even here we seem to have a reason (at least for small $k$) to claim that $k$-AmbNN is more robust regarding the increasing values of $k$. We cautiously suggest that the experiments with the first two domains indicate that $k$-AmbNN offers not only higher performance, but also higher robustness with respect to $k$. Note that, somewhat surprisingly, the fuzzy approach again does not show its strength.

In the remaining experiments, we modified our system so that it automatically chooses the optimum $k$ value. This is achieved by an “induction” algorithm that estimates the classification accuracy (applying the 5-fold cross-validation approach to the training set) for different values of $k$ and then selects the one that promises the highest performance. The same approach could in principle have been employed also for the choice of the $\theta$-threshold used in the voting scheme but we used the fixed $\theta = 0.3$ not to complicate things.

Figure 5 shows how the classification performance depended on the amount of ambiguities in the data. While $k$-fuzzyNN and $k$-NN appear relatively unperturbed by this parameter, $k$-AmbNN's performance drops conspicuously with growing values of $AAmb$. The observation leads us to assume that $k$-AmbNN is more appropriate where the domain ambiguity is limited.

Conclusion

Having surmised that classical nearest neighbor classifiers may be inadequate to deal with ambiguously described examples, we proposed our own modification, $k$-AmbNN (ambiguous nearest neighbor), and compared its performance with that of the classical $k$-NN rule and with that of a solution suggested by the fuzzy-sets community.

Importantly, we have realized that ambiguous domains call for a specially designed performance metric. Our experiments with three different domains indicate that the performance of the $k$-AmbNN compares very favorably with the performance of modest modifications of the classical $k$-NN classifier and with $k$-fuzzyNN. While $k$-NN apparently suffers from the replacement of partial ambiguity with the “don’t know” symbol, $k$-fuzzyNN seems to have been meant for more sophisticated uncertainties than those encountered in our domains.

The reader may complain that the paper fails to report experiments with an impressive array of benchmark domains as is common in the machine-learning literature. The truth is that we found in the UCI repository only one such domain, university. We speculate that other UCI domains might originally have contained ambiguities, too, but their authors sanitized them because the community was only used to totally unknown attribute values. However, the experience re-
ported in this paper indicates that the fact that, say, season is either spring or summer—but not fall or winter—is qualitatively different from the “question-mark” situation.

Finally, our work suggests there is a need to search for better methods to quantify such aspects as the degree of data ambiguity. To this end, we have proposed our own formula but we hope that other researchers will scrutinize its shortcomings and limitations, and, if necessary, develop more appropriate methods. The same applies to the formula we have used to assess the classification performance.

This brings us to suggestions for further research. In an attempt to make the paper self-contained, and to avoid advanced theoretical paradigms that might obscure the simple ideas and observations we wanted to share, we labored hard to make our solution as simple as possible. However, more sophisticated approaches can be employed even in the unassumming paradigm of nearest-neighbor classifiers. For instance, the fuzzy-set theory (Bezdek) certainly offers many more possibilities than the one from (Keller). Also the voting mechanism could have relied on sounder theoretical principles such as those developed in the frame of the Dempster-Shafer theory. For an early attempt to employ this paradigm in domains with ambiguous class labels (but not attribute values), see (Denoeux).

Finally, we would like to encourage work in other fields of machine-learning. In the realm of decision trees, the pioneering research reported by (Vannoorenbergh; Vannoorenbergh and Denoeux) has suggested theoretical solutions that still lack systematic experimental evaluation. We are sure that other frameworks—such as linear classifiers, Bayesian classifiers, neural networks, or support vector machines—offer a rich source of opportunities that, lamentably, no one has yet attempted to explore. Our paper hopes, in its modest way, to help change this situation.

For the code of the algorithms used in this paper, as well as for the experimental data we have used, please contact Hans Holland—hholland@miami.edu.

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References


