Abstract
An automated procedure for protein design by optimization of a sequence-structure quality has been developed. The method selects a statistically optimal sequence for a particular structure, on the assumption that such a protein will adopt the desired structure. We present two optimization algorithms: one provides an exact optimization while the other uses a combinatorial technique for comparatively rapid results. Both are suitable for massively parallel computers. A prototype system was used to design sequences which should adopt the four-helix bundle conformation of myohemerythrin. These appear satisfactory to secondary structure and profile analysis. Detailed inspection reveals that the sequences are generally plausible but, as expected, lack some specific structural features. The design parameters provide some insight into the general determinants of protein structure.

Introduction
Despite decades of research, our present understanding of protein structure is still incomplete. While structural analysis has yielded many of the fundamental rules governing the general architecture of protein folds (Chothia & Finkelstein 1990), it has been limited by the relatively few known protein structures and the fact that they have been limited by evolution (Pastore & Lesk 1991). Therefore, mutation analysis has become one of the most powerful tools for studying the structure of proteins and has provided a wealth of information about particular folds. However, this data has left unanswered many general questions about the large-scale structural features of proteins. The most clear evidence of our imperfect knowledge of protein structure is that the protein folding problem remains largely unsolved: we cannot determine the conformation a protein will adopt from the knowledge of its sequence alone.

Protein design has emerged as a promising technique for understanding protein structure because finding a sequence which will fold into a desired structure may be considerably simpler than computationally folding a sequence into a structure (Yue & Dill 1992). In addition to providing new scientific knowledge, new proteins have potential uses in biotechnology and medicine.

Many groups have taken up the challenge of building new proteins using “physical, statistical, and intuitive criteria” (Sander 1991) in a procedure called design by modeling (Brenner 1994). The four-helix bundle is one of the most popular structures being designed (Regan & DeGrado 1988; Hecht et al. 1990; Hill et al. 1990; Sander et al. 1992a; Schafmeister et al. 1993), and such one structure has been proven correct by crystallography. A related designed protein, consisting of two antiparallel alpha-helices, has had its structure solved by NMR (Kuroda et al. 1994). Attempts have also been made to build other structures (Sander et al. 1992b) including alpha-beta barrels (Goraj et al. 1990; Tanaka et al. 1994), a beta bend (Richardson & Richardson 1987), and a crystallin (Hubbard & Blundell 1989), as well as some folds not occurring in nature such as a miniature antibody (Pessi et al. 1993) and an alpha-beta “open sandwich” (Fedorov et al. 1992).

The success of several of these experiments has been encouraging and the partial failures have frequently been instructive. However, the manual procedure used to design the proteins means that the procedure is fundamentally irreproducible: the knowledge used to build one protein cannot be directly applied to the construction of another.

Some experimentalists have gone to the opposite extreme and made random sequences of amino acids either with hydrophobic/hydrophilic patterns (Kamtekar et al. 1993) or a limited set of residues (Davidson & Sauer 1994). While intriguing, these “design” experiments cannot be directly used to select single proteins which should adopt a given fold. However, some systems have been developed to find proteins sequences which meet particular criteria. Ponder and Richards designed sequences whose side chains could adopt acceptable rotamer positions and pack densely (Ponder & Richards 1987), while Yue and Dill found binary sequences of polar and non-polar residues which would form more hydrophobic contacts in the desired structure than in any alternative structure (Yue & Dill 1992).
A Quantitative Methodology

We have created a quantitative methodology which attempts to combine the comprehensibility and success of the design by modeling experiments with the reproducibility of the more general methods. It relies principally on the statistical features of all known protein structures to form a function which measures the compatibility of given sequence and structure. This function is then optimized over a selected structure to produce an "ideal" sequence for that fold. Thus, the procedure can be easily repeated any number of times on any structure.

The parameters entering into sequence-structure quality function, detailed elsewhere (Brenner & Berry 1994), can be divided into four main categories: position, neighbor, uniqueness, and hints. The first two are the main contributors to the design procedure and are statistically based. Position preferences describe the preference of a given amino acid for particular position within a protein (e.g., lysine is well suited for a solvent exposed helical position). The statistical tendency for two or more amino acids, such as leucine and valine, to be near each other falls within the neighbor preferences category. Uniqueness is a parameter which attempts to ensure that the designed sequence will be comparatively unstable in folds other than the desired one (Yue & Dill 1992), and hints incorporates a wide variety of details which are specific to the protein being designed, such as large motifs and functionality.

To form the evaluation function, each parameter is weighted according to its relative importance and summed with the others. This means that an arbitrary number of detailed criteria can be incorporated in the design system and that the method can be extended and modified as both experimental results and theoretical research provide additional information.

Optimization Methods

Ternary Division Sum Optimization

One Dimension. The optimization of a sequence-structure quality function containing position preferences is trivial: at each position select the best residue (e.g., by table lookup). So long as they are not overly complex, the uniqueness and hints criteria serve only as masks limiting the residues at particular positions. Thus, their inclusion does not increase the computational complexity of the design task.

Unfortunately, the neighbor preferences complicate sequence selection considerably. If the residue at each position interacts with the residues at every other position, then the optimization procedure requires the evaluation of every potential sequence—an exponential time procedure. Indeed, this exponential complexity is one of the major

Figure 1. General, automated protein design. The quantitative protein design methodology accepts any plausible protein structure and selects a sequence which should be stable in that configuration. The figure is by M. Elms.

Figure 2. Pseudocode for the 1-dimensional TDSO algorithm. To optimize a function of n residues i...n, with position and neighbor preferences specified by the functions g and h, respectively, run tds0(0, n+1, L, R), where L and R are the left and right endcaps. This will return the optimal sequence and its score.
barriers to computational protein folding. However, one of the principal reasons that protein design may be a computationally easier task than protein folding is that the positions of all the residues are known in advance. Thus, interactions between residues which are distant in sequence need only be considered if the residues are close in space. In one dimension, the evaluation function $F$ (with an implicit structure) over a sequence $S$ has the form:

$$F(S) = \sum_{i=1}^{N} g(i, s_i) + \frac{1}{2} \left( h(s_{i-1}, s_i) + h(s_i, s_{i+1}) \right)$$

where $s_i$ is the residue at position $i$, $g(x, u)$ is the position preference of residue $u$ at position $x$, and $h(u, v)$ is the neighbor preference of residues $u$ and $v$.

A procedure for optimizing position and neighbor preferences in one dimension was developed by Steven P. Ketchpel (personal communication). A considerably more efficient version of this algorithm, ternary division sum optimization (TDSO), has been developed and its complexity analyzed. The principle underlying TDSO’s operation is that the optimal sequence is that which has the best beginning, middle, and end. Pseudocode for the algorithm is provided in Figure 2 and its operation is diagrammatically portrayed in Figure 3.

TDSO begins with a sequence that has left and right end-caps. Then it computes the position preference for each of the 20 types of residue at the central location. To each of these it adds the recursively computed qualities of the left and right sides using the current central residue as the right and left end-cap, respectively, for these sides. Recursion is ceased when no central position can be selected, and the remaining neighbor preference is computed. The algorithm is $O(n k \log n)$ where $k$ is the number of amino acids, 20, to be considered. Thus, the single-dimension procedure is polynomial and, although it is high order, is generally tractable for relatively small $n$.

Many Dimension. When TDSO is extended beyond one dimension to an arbitrary graph, it is impossible to pick a center pivot position which will divide the graph into two disjoint ones. Instead, it is necessary to find a set of nodes which together partition the graph into two subgraphs, as shown in Figure 4. However, instead of needing to test $k$ residues at the center position at each recursive level, it is necessary to test all combinations of residues at these positions. If there are $m$ border nodes, then $k^m$ different partitions must be tested and summed with the best "left" and "right" subgraphs. As expected, the complexity of the algorithm increases as the connectivity increases. The graph version of the algorithm is $O(n k (\log n)^c)$ where $c$ is a measure of the connectivity of the graph and typically is a function of $n$. For example, $c$ is $n^{(d-1)/d}$ for a regular grid of dimension $d$. Therefore, the complexity of TDSO grows exponentially as a root of $n$ making this procedure unfeasible except for trivial cases.

However, though the running time of this algorithm grows dramatically with sequence length, it may still be tractable if various approximations are applied, including alpha/beta cutoffs (Horowitz & Sahni 1978; Aho et al. 1983) and heuristics that reduce $k$, the number of choices at each position, from 20 residues to just a few classes (e.g., hydrophobic, polar, and neutral). Moreover, the main foreach loop in TDSO is straightforward to parallelize, and with the exception of the selection of the best middle residue, no communication is necessary. Consequently, near-ideal speedup on massively parallel computers should be easy to achieve.

Simulated Annealing

While the exact optimization provided by TDSO is essential for verification of results, it is too time consuming when the design procedure is being developed and extended. For this reason, combinatorial optimization methods have been used to design sequences with a prototype sequence-structure quality function. In particular a straightforward simulated annealing protocol (Metropolis et al. 1953; Press et al. 1988) and several variants have been applied.

Serial. On a single processor, a sequence can be optimized for a particular structure by iterating over the sequence and randomly mutating residues at each position to any other residue. After each change, the modified sequence is
analyzed by the sequence-structure evaluation function and the mutation is accepted or rejected according to the variation in quality and the current temperature.

The parameters selected for the model system (below) caused the system to be cooled too quickly to converge to a single designed sequence. However, the different sequences generated from each set of parameters showed no significant difference in quality. Moreover, while (nearly) every natural protein adopts only a single structure, any given natural structure can be formed by several different sequences. Thus it is unnecessary to select the best possible sequence as stipulated by the objective function; near-optimal sequences will provide satisfactory results. Indeed, since the margins of error in the various rules which contribute to the overall methodology are considerable, the best sequence computed by the statistics is unlikely to optimize the underlying parameters that the statistics attempt to describe. In addition, the variable residues in the sequences designed with similar criteria help provide some insight into which positions are most constrained by the quality function.

Parallel. While the serial Metropolis method can produce results very quickly for small proteins with easily computable quality measures, it becomes inconvenient when working with large proteins and complex objective functions. Even in these complex instances, the computational design procedure is much faster than actually synthesizing the designed protein. However, to develop, test, and improve the design methodology, it is necessary to generate large numbers of sample sequences. Therefore, methods to increase the speed of designing new sequences are of considerable practical utility.

Because the quality function $F$ is the sum of the qualities of each of the individual positions (although each position’s quality depends on its neighbors), it is not difficult to parallelize the simulated annealing algorithm. One method of implementing this is to block partition the sequence evenly across the compute nodes of the parallel computer. Because of the neighbor preferences, every node needs to keep a record of the current neighbors of all of the positions which it is trying to optimize. Therefore, as shown in Figure 5, each node has an array storing the whole sequence and “imagines” that it knows the entire sequence at the current level of annealing. However, each optimizes only the small subset of the sequence assigned. To be isomorphic with the serial optimization algorithm, synchronous communication must be used. That is, each node must wait until it has received messages containing information about the current neighbors before proceeding with the annealing. Coded this way, the parallel algorithm does provide significant speed enhancement over the serial one in many cases. However, as the number of neighbors increases, the communication overhead grows dramatically.

**DUPSA.** For this reason, an asynchronous version of the optimization procedure has also been developed. In this

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**Figure 5.** Schematic of DUPSA data distribution. Boxes are the sequence, and the large circles show segments of sequence to be optimized by a single node. Small circles show position preferences and double headed arrows, neighbor preferences. Open-headed arrows show where communication is necessary.

**Figure 6.** Pseudocode for the DUPSA algorithm. Prior to running dupsa, each node has the global variables left and right set to delimit the regions of sequence to be optimized. Thus, on each node, positions left...right of the array sequence are selected by the optimization procedure. Positions of sequence outside this region are filled in by the asynchronous receive messages from neighbor nodes, and those positions which do not neighbor the region being optimized have random values. Following dupsa, each node must send the region of sequence it optimized to a leader node which collates the information. A considerable amount management detail has been omitted for clarity. Full source is available from SEB.
algorithm (Figure 6), called delayed update parallel simulated annealing (DUPSA), messages about residue positions are sent to nodes containing their neighbors only if there has been a change. More importantly, each compute node optimizes its sequence with the most recently received information rather than waiting for messages with the most current neighbors to be received. This means that computation continues during the communication delay between when a neighbor residue changes and when this change is registered. As shown in Figure 7, even for with the simple prototype quality function (see below), there was a significant speedup over the serial algorithm when using this procedure, although for very small proteins the communication overhead still becomes predominant when more than two processors are used. However, when a (hypothetical) more complex is employed and multiple annealings are run in parallel, up to 100 compute nodes can be profitably used for even very small proteins.

There was some concern that the time period between residue change and update at neighbor nodes could potentially be problematic. However, for the design systems tested, this gap where out-of-date neighbor information is used had no detrimental effect on the final sequences. Thus, the DUPSA selects sequences as well as the serial simulated annealing protocol in a fraction of the time. Moreover, DUPSA is general enough to be applied to any similar optimization where local interactions are present.

A Model System

A model system containing only a few of the parameters in the full methodology has been used to evaluate the potential of the quantitative methodology (Brenner 1993; Brenner & Berry 1994). By formulating an evaluation function which incorporates only naive secondary structure, solvent accessibility, and primary structure neighbor preferences, we did not expect to produce a system which would produce reasonable sequences. However, the model system which operates on those parameters, as well as a hint (called diversity) to force the composition of the designed sequences to reflect that of the SwissProt database (Bairoch & Boeckmann 1991), has done surprisingly well. The system has been used to design sequences for phage 434 Cro (Brenner 1993; Brenner & Berry 1994), hemoglobin, two SH3 domains (Brenner 1994), lactate dehydrogenase, and ubiquitin. Here we present new sequences to adopt the fold of Themiste zostericola myohemerythrin (Sheriff et al. 1987), as represented by the coordinates in PDB entry 2mhr.

Myohemerythrin is perhaps the canonical four-helix bundle, with four long, well formed helices. The natural protein binds oxygen through two irons which are coordinated by several histidines. However, no rules for ligand binding or other functionality were incorporated into the model design system used to select these sequences.

Designed Sequences

To explore the range of the design system and to gain a better understanding of the relative importance of its constituent parameters, a wide variety of different parameter weightings were used in designing the sequences shown in the Sequence Table. Thus some sequences were built using secondary structure preference almost exclusively (e.g., 44-46), while others were mainly selected on the basis of solvent accessibility (as in 47 and 48). However, most sequences were designed using a mix of all four parameters.

When inspected, most sequences appeared normal, aside from a possible excess of certain residues such as lysine and alanine. However, few sequences, particularly those selected with a strong bias towards secondary structure, look positively bizarre because of their extremely biased residue composition. Intriguingly, none of the designed proteins showed significant homology (p<0.001 for blastp (Altschul et al. 1990) with the seg filter and match matrix on the May 1994 nr database) to any natural proteins. As a test of the sequences' propensity to adopt the correct local structure, they were subjected to secondary structure prediction (Rost & Sander 1993; Rost et al. 1994) and scored on how well the predicted structure matched the desired structure. Perhaps surprisingly, nearly all produced very good results; indeed, the designed sequences generally scored higher than the native.

Structural Models

In addition, structural models were made threading the designed sequence onto the structure of the natural myohemerythrin structure, using the method in (Brenner & Berry 1994). A schematic view of the natural and a designed protein (Figure 8), shows that the selection of residues looked reasonable, although, the packing between the helices was much looser in the designed sequence than in the natural. In addition, none of the many hydrogen-bonded turns in the natural sequence appeared in the designed sequences. However, since that no information about either
Figure 8. *Themiste zostericola* myohemerythrin structure (coordinates from PDB entry 2mhr) threaded with natural and designed sequences. The natural protein is shown in A, while a model has been constructed by threading a designed sequence (Sequence Table, line 1) onto the 2mhr backbone in B. The force field used for generating the structural model from the designed sequence contained an error which results in misshapen aromatic residues.

of these features was included in the optimization function, these results were expected.

What is more surprising, however, is how well the designed sequences fared when the structural models were analyzed with environmental profiles (Lüthy et al. 1992). Most scored about as well as the native structure and none of the sequences failed this verification assay.

In general, these uniformly positive evaluations of the designed sequence over a extraordinary range of different weightings agree with the results found for the all-helix Cro protein. It may be that this indicates that all weightings are acceptable. However, it seems more likely that the evaluation techniques used simply fail to differentiate between some good and poor sequences. If this is the case, then selecting appropriate weightings will be one of the most challenging tasks in constructing fully successful quantitative design systems. Nonetheless, some quality variation is visible, and can be exploited to ensure that experimentally constructed proteins have the optimal set of weighted parameters. Moreover, data culled from beta sheet proteins, which show more variation in quality (Brenner 1994), can also be used to tune the design system.

**Conclusion**

Protein design is a challenging task which provides a new way of understanding protein structure and has practical utility. However, most work in this field has been irreproducible and unverifiable because of the qualitative and intuitive nature of the design process. We have presented a quantitative methodology which automatically designs proteins by optimizing a sequence-structure quality function over a particular structure to yield an optimal sequence. With the parallelizable supporting algorithms, the task is relatively quick and amenable to exploration. Indeed, a model system containing only a few criteria has already designed sequences which score well according to secondary structure and tertiary structure evaluation.

We are initiating the essential experimental work to synthesize and characterize proteins designed by the quantitative system. Concomitantly, more sophisticated versions of the protein design system are being constructed. If successful, the method will be able to generate new proteins with pre-determined structure and confirm the relationships between statistically observed features of proteins and their relative structural importance.

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Brenner
**Designed Sequence**

Lines a shows the natural protein sequence and b lists the crystallographically assumed secondary structure (H: helix; E: sheet; L: loop).

**Sequence Table.** Sequences designed to adopt the fold of *Themiste zostericola* myohemerythrin fold (Sheriff et al., 1987), PDB entry 2mhr.

- **Prediction column** (lines 1-50) shows how well the sequences' secondary structure prediction agreed with the desired secondary structure derivative column; from darkest to lightest, the regions represent the relative weighting, on an arbitrary scale, of secondary structure preference, solvent accessibility preference, primary structure neighbor preference, and diversity. The **Prediction column** (lines a, 1-50) shows how well the sequences' secondary structure prediction agreed with the desired secondary structure.
Derivation Prediction Profile

Native Structure Sequence Numbers

5EKIGGLSAPVDAKNVDYCEWLVHINIGTDFKRYGKL

Myohemerythrin

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on line b. The score here was computed by adding two points for every position which was predicted to have the correct structure and deducting one for every position which was predicted to have an undesired structure. For scale, line b shows the score that would be received by a perfect prediction. The Profile column shows how well the structural models of the designed sequences rate in a profile analysis. The bars show by how much the assigned score exceeds the minimum quality cutoff of 24.0. The profile score of the natural myohemerythrin is 48.8.

Brenner 51
References