Abstract
Conventional document retrieval systems (e.g., Alta Vista) return long lists of ranked documents in response to user queries. Recently, document clustering has been put forth as an alternative method of organizing retrieval results (Cutting et al. 1992). A person browsing the clusters can discover patterns that could be overlooked in the traditional presentation.

This paper describes two novel clustering methods that intersect the documents in a cluster to determine the set of words (or phrases) shared on experiments that evaluate these intersection-based clustering methods on collections of snippets returned from Web search engines. First, we show that word-intersection clustering produces superior clusters and does so faster than standard techniques. Second, we show that our \(O(n \log n)\) time phrase-intersection clustering method produces comparable clusters and does so more than two orders of magnitude faster than all methods tested.

Introduction
Conventional document retrieval systems return long lists of ranked documents that users are forced to sift through to find the relevant documents. On the Web, this problem is exacerbated by the high recall and low precision of search engines (e.g., Alta Vista). Moreover, the typical user has trouble formulating highly specific queries and does not take advantage of advanced search options. Finally, this problem gets worse as the Web continues to grow.

Instead of attempting to reduce the number of documents returned (e.g., by filtering methods (Shakes, Langheinrich, & Etzioni 1997)) we attempt to make search engine results easy to browse. We investigate document clustering as a method that enables users to efficiently navigate through a large collection of documents. In addition, clustering enables the user to discover patterns and structure in the collection that could be overlooked in the traditional ranked-list presentation. In this context, a document clustering method requires:

1. **Ease-of-browsing**: A user needs to determine at a glance whether a cluster's contents are of interest.
2. **Speed**: Web users expect results within seconds.
3. **Scalability**: The method should be able to quickly cluster thousands of documents.
4. **Snippet-tolerance**: The method should produce "reasonable" clusters even when it only has access to the short document snippets returned by the search engines; most users are unwilling to wait for the system to download the original documents.

In this paper we describe and experimentally evaluate two novel clustering methods that meet the above requirements to varying degrees.

Document Clustering
Document clustering has been traditionally investigated mainly as a means of improving document search and retrieval. Recently, a technique named Scatter/Gather (Cutting et al. 1992) introduced document clustering as a document browsing method. Our work follows the same paradigm.

Hierarchical agglomerative clustering (HAC) algorithms are the most commonly used methods for document clustering (Willet 1988). These algorithms start with each document in a cluster of its own, iterate by merging the two most similar clusters, and terminate when some halting criterion is reached.

HAC algorithms require the definition of a similarity function between documents and between sets of documents. Each document is typically represented as a weighted attribute vector, with each word in the entire document collection being an attribute in this vector. The similarity of two documents is often taken as a normalized function of the dot product of their attribute vectors.

Several halting criteria for HAC algorithms have been suggested (Milligan & Cooper 1985), but they are typically based on predetermined constants (e.g., halt when 5 clusters remain). Because the HAC algorithm
does not backtrack it is very sensitive to the halting criterion — when the algorithm mistakenly merges two “good” clusters, the resulting cluster could be meaningless to the user. In the domain of search engines, we often receive many irrelevant snippets — snippets that do not have any correlation to the query or to other snippets. This sort of “noise” reduces even further the effectiveness of commonly-used halting criteria.

HAC algorithms are typically slow when applied to large document collections. Single-link (Rijswijk 1971) and group-average methods typically take $O(n^3)$ time\(^1\), while complete-link methods typically take $O(n^3)$ time (Voorhees 1986b). In terms of quality, on the other hand, complete-link algorithms have been shown to perform well in comparative studies of document retrieval (Voorhees 1986a), as they tend to produce “tight” clusters — clusters in which all the documents are similar to one another. Single-link, and to a lesser degree group-average methods, exhibit a tendency toward creating elongated clusters. Elongated clusters have the undesirable property that two documents can be in the same cluster even though the similarity between them is small. From our experience in the Web domain, algorithms that produce elongated clusters often result in one or two large clusters, plus many extremely small ones. This can lead to non-intuitive clusters.

The above discussion suggests that traditional document clustering methods fail to meet the requirements listed in the introduction. Often, the methods generate elongated clusters that are not easy to browse — it’s difficult to determine at a glance what the contents of a given cluster are likely to be. Furthermore, $O(n^3)$ time clustering is likely to be too slow for Web users when $n \geq 1,000$ or more. Finally, our experience shows that standard techniques perform poorly on the short and “noisy” snippets of Web documents.

**Word-Intersection Clustering**

Word-intersection clustering (Word-IC) is a new method designed to address some of the problems mentioned above. Word-IC results in “tight” clusters, has a well motivated halting criterion and captures a desirable trade-off between the number of clusters, their size and their cohesion.

Word-IC is a HAC algorithm that relies on a novel Global Quality Function ($GQF$) to quantify the quality of a clustering. We use the $GQF$ as the heuristic to guide the HAC algorithm and as the halting criterion. At each iteration of the HAC algorithm, the two clusters whose union would result in the highest increase in the $GQF$ are merged. The algorithm terminates when no merge increases the $GQF$. Next we’ll describe the $GQF$.

The definition of a cluster’s cohesion is central to the $GQF$. We define the cohesion of a cluster $c$ as the number of words common to all the documents in the cluster. We define the score $s(c)$ of a single cluster $c$ to be the product of its size $|c|$ and its dampened cohesion. The score of a singleton cluster is defined to be 0.

For a clustering $C$, the $GQF(C)$ is a product of three components: (a) $f(C)$ — A function proportional to the fraction of documents in non-singleton clusters. This component captures the notion that singleton clusters are “bad”. (b) $1/g(|C|)$ — Where $g(|C|)$ is an increasing function in the number of non-singleton clusters. This component captures the notion that the fewer clusters there are, the better. (c) $\sum_{c \in C} s(c)$ — The sum of the scores of all clusters in the clustering. Thus:

$$GQF(C) = \frac{f(C)}{g(|C|)} \sum_{c \in C} s(c) \tag{1}$$

Notice that the factors $1/g(|C|)$ and $\sum_{c \in C} s(c)$ create a tension between two extremes: having a small number of large clusters of low cohesion vs. having many small clusters of high cohesion. The $GQF$ provides a trade-off between these two extremes. We have investigated different functional forms for the components of the $GQF$; our experiments have revealed that good results are obtained if $f(C)$ is simply the ratio of the number of documents in non-singleton clusters to the overall number of documents, and $g(|C|)$ is the number of non-singleton clusters raised to the power of 0.5.

Word-IC can be performed in $O(n^2)$ time. The result is a monothetic classification: all the documents in a given cluster must contain certain terms if they are to belong to it. In Word-IC, that set of common words — the centroid of the cluster — can be presented to the user as a concise description of its contents. We believe that this approach results in high-quality clusters because all the documents in the cluster share at least the words in its centroid.

Experimental results in section 5 show that Word-IC is faster and results in higher quality clusters than the commonly used group-average HAC algorithm using the cosine inter-document similarity function.

**Phrase-Intersection Clustering using Suffix Trees**

Following the standard document clustering paradigm, Word-IC treats a document as a set of words, disreg-
arding word sequences. We conjecture that word proximity information may be valuable in some cases. Furthermore, clusters whose centroid is a shared phrase would be particularly easy to browse. Based on these observations we formulate Phrase-intersection clustering (Phrase-IC) — a novel intersection-based approach that looks at the phrases that are common to a group of documents as an indication of the group's cohesion.

The HAC algorithms mentioned previously have \(O(n^2)\) time complexity, an obstacle to our speed and scalability goals. Phrase-IC using suffix trees (Weiner 1973) is an \(O(n \log n)\) time algorithm that results in a large speedup without much degradation in quality.

The suffix tree of a set of strings is a compact trie containing all the suffixes of all the strings. In our application, we construct a suffix tree of all the documents. Each node of the suffix tree represents a group of documents and a phrase that is common to all of them; the label of the node represents the common phrase, and all the documents who have corresponding leaves that are descendants of the node make up the group. Therefore, each node can be viewed as a potential cluster. Each node is assigned a score that is a function of the length of the phrase, the words appearing in it, and the number of documents in that cluster. The nodes are sorted based on their score.

Clusters are determined directly from this sorted list of potential clusters using a simple selection algorithm. Notice that the selected clusters may overlap. We believe that this feature is advantageous to the user, as many topics do overlap. When selecting which clusters to display, we make sure the overlap between the selected clusters is not high. We are currently exploring the option of merging potential clusters with high overlap.

The space requirement of the suffix tree is \(O(n)\), and it can be constructed in \(O(n)\) time (Ukkonen 1995). The suffix tree can be built incrementally as the documents arrive. This allows the use of "free" CPU cycles as the system waits for additional documents. The number of potential clusters is \(O(n)\), thus sorting them and selecting which to present to the user can be performed in \(O(n \log n)\) time.

**Preliminary Experiments**

It is hard to measure the quality of a clustering algorithm, as one has to know the "correct" clustering of the test cases. We chose to apply the algorithms to snippet collections created by merging several distinct base collections. We then scored the resulting clustering by measuring its deviation from the original partition of the snippets into base collections.

We created 88 base collections from snippets returned by MetaCrawler (Selberg & Etzioni 1995) in response to 88 different queries. Each of the queries contained between 1 and 4 keywords and defined a topic in computer science (e.g. kernel & architecture; biology & computational; compiler). Each base collection contained approximately 120 snippets; each snippet contained 40 words, on average. Test collections were created by merging 1 to 8 randomly chosen base collections, giving us test collections ranging from 120 to 1000 snippets in size. 20 test collections of each size were created, for a total of 200 test collections.

We need a scoring method to compare the original partition of the snippets into base collections with the algorithm generated clustering. To do so, we look at all pairs of documents in a single cluster, and count the number of true-positive pairs (the two documents were also in the same base collection) and false-positive pairs. The quality of the clustering is a function of the difference between these two quantities, normalized by the size of the collection clustered. A quality score of 1 means a perfect reproduction of the original partition.

![Figure 1](image.png)

Figure 1: (a) The quality of the clusters produced by the different algorithms. (b) The execution time of the different algorithms. The execution time of the Phrase-IC algorithm cannot be seen on the scale shown, as it clusters 1000 snippets in less than 0.5 seconds. This algorithm exhibits a good tradeoff between quality and speed — it achieves high quality clusters in \(O(n \log n)\) time.
We are currently deploying a clustering module on top of MetaCrawler, which will enable us to conduct user studies aimed at answering these questions empirically.

Conclusion

We have described and experimentally evaluated two novel clustering methods that enable users to quickly navigate through the results of Web search engines: word- and phrase-intersection clustering. Phrase-IC using suffix trees is an \(O(n \log n)\) time algorithm that appears promising in terms of the stringent requirements outlined in the introduction including ease of browsing, speed, and scalability. Of course, additional experiments and extensive user studies are necessary before definitive claims can be made about the performance of our algorithms in practice.

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References


