Improving Sketching by Utilizing Haptic Feedback

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Abstract
Sketching interfaces for PC’s often make use of the mouse. This device, however, is not suitable for the creation of “good” gestures. This paper describes the use of a PHANToM device, a force feedback device, for making sketches on a computer. This device has a pen-like appearance and is therefore natural to use. The paper elaborates on algorithms for the use of the force feedback capabilities of the PHANToM device in a sketch interface. The algorithms for creating and modifying sketches will be discussed, together with the algorithms for feeding force back to the user.

Introduction
Over the past few years, a number of sketching interfaces, such as Teddy (Igarashi, Matsuoka, & Tanaka 1999) were developed in order to generate curves that could be easily interpreted. For instance, Teddy generates 3D information out of 2D sketches. Most of these computer programs focus on all three dimensions, mainly because curves are a starting point for developing surface manipulation tools. Sánchez-Reyes (1997) created a tool for NURBS modification. Recently, pen input is used in gesture interfaces for PDA’s (Long et al. 2000; Mankoff, Hudson, & Abowd 2000). However, most programs, which provide 2D sketching input, only allow mouse interaction, which is not natural for most users: even experienced computer users find it difficult to sketch using a mouse. An alternative is the use of a graphics tablet, which provides a natural and intuitive sketching interface and is therefore preferred over the use of a mouse. An extension of this interaction device is the pressure-sensitive tablet, because it provides a means to vary the width of the lines that are being drawn and acts as a physical haptic constraint.

However these methods cannot support a intuitive means to edit the lines that are being drawn in case the user is not satisfied with his sketches. We propose the use of haptic feedback to draw and edit sketches. Our algorithms use a mathematical representation of the sketches, which can both be used for editing the curve and providing feedback. This solution has as advantage that this mathematical representation is calculated in real-time and can therefore easily be used in a processing algorithm. Our own processing algorithms that change the sketch make use of the benefits of this representation. Other process algorithms that can for instance create 3D out of the sketches or allow the sketches to be animated, can also make use of our mathematical representation, since it applies well-known mathematical techniques.

This paper explains the use of force feedback and elaborates on the benefits of this approach. The algorithms used in our tool will be discussed, but this discussion focuses on the integration of force feedback in the sketching tool. For a thorough explanation of the remainder of the algorithms, we refer the interested reader to the paper by Vansichem, Wauters, & Van Reeth (2001).

Force Feedback
Force feedback devices are devices that are able to generate forces which can be fed back to the user. This force feedback affords the user to feel objects that only exist in the virtual world. At this moment, most of the commercially available force feedback devices can either provide force feedback, such as the iFeel MouseMan (Logitech 2001), or give full 3D force feedback, such as the PHANToM haptic master (Massie & Salisburg 1994) which is depicted in figure 1.

Figure 1. PHANToM device

At this moment, only a few haptic devices are commer-
cially available. Most of the time, the PHANToM haptic master is used in research and industry. To a lesser extend, the FCS HapticMASTER (FCS Control Systems 2001) and the Delta Haptic Device (Grange et al. 2001) are used as an alternative for the PHANToM device. In our research, we use the PHANToM device (as depicted in figure 1), which provides 6D input and 3D output. Although the PHANToM device is created for tasks in 3D space, it has successfully been used in 2D environments (e.g. Miller & Zelevnik 1998).

Force feedback, which is the mechanical production of information sensed by the human kinesthetic system (Oakley, McGee, & Gray 2000) is a form of haptic feedback which relates to the sense of touch. These terms are often interchanged.

This paper discusses the algorithms used to calculate the forces which are fed back through the PHANToM device; a more thorough explanation on haptic rendering can be found in (Ruspinii 1999).

**Sketch Creation**

In order to easily manipulate a sketch, the individual pixels are grouped together into segments. Each of these segments is represented by a cubic Bézier spline, as depicted in figure 2. The control points in this figure are shown for illustrative purposes only, our users are not confronted with these control points; they directly manipulate the sketch.

These cubic Bézier splines are defined by equation 1.

\[
f(t) = (1-t)^3B_1 + 3t(1-t)^2B_2 + 3t^2(1-t)B_3 + t^3B_4 \quad (1)
\]

By applying curve fitting techniques, the pixels are added to the current segment. Whenever the least square error of the curve fitting passes a preset threshold, a new segment is created. In order to provide smoothness of the sketch, two subsequent segments share a number of pixels. A new segment is created by determining the control points \(B_1\), \(B_2\), \(B_3\) and \(B_4\) so that the difference between the spline and the corresponding data points \((P_1, P_2, \ldots, P_n)\) is as small as possible. The start and end point \((B_1\) and \(B_4))\) of the spline can be chosen in function of the above-mentioned smoothness represented by the parameter \(s\): the number of shared data points.

\[
B_1 = P_{s} \quad \quad B_4 = P_{n-s} \quad (2)
\]

The two other control points \((B_2\) and \(B_3))\) can be constructed by means of least square minimization (Vanschem, Wauters, & Van Reeth 2001).

The use of force feedback helps to improve the “correctness” of the sketch: when using force feedback, one can be sure that all pixels are taken into account. The input device for the sketch creation has to be sampled by the program; for common input devices, like the mouse, this sampling occurs at a small rate, so when the user moves fast, the sampling process can skip pixels, which leads to cruder sketches. On the other hand, most force feedback devices are accessed in a high-priority loop. This loop is executed at a rate of 1kHz in order to generate realistic forces. Using a real-time operating system a rate of even 5kHz can be obtained (Kabelić 2000). The position of the force feedback device can also be sampled in this loop, resulting in a smooth sketch, even if the user moves very fast. Since the PHANToM device has a sub-millimeter resolution (0.03mm), we do not use all sampled positions, but use a threshold to determine when a new data point has to be created.

At this creation stage, force feedback is primarily used to guide the user: a haptic plane is defined onto which the user can draw the sketches. When the user presses harder against this plane, a thicker line is drawn, like would happen when using paper and pencil. Different surfaces can easily be simulated by altering this resistance, an effect that cannot be achieved using conventional input devices.

**Controlling the Width**

A planar constraint effect is used in order to restrict the movement of the PHANToM device in the z direction. However the stylus can be moved slightly in the z direction by exerting a force in this direction. This information is used to determine the width of the curve: the harder the user pushes, the wider the line is drawn. In contrast to the position of the data points, which are determined using Bézier interpolation, the line width at the points is calculated using a linear interpolation. The line width of the curve is thus represented as set of interconnected line segments.

\[
W = (1 - t_w)W_1 + t_wW_2 \quad (3)
\]

\(W_1\) and \(W_2\) represent the width at the start and end of the segment. The \(t_w\) value, which is used to determine the width at the point, can be determined using the \(t\) value which is used to calculate the position of the point, as described in the previous section. But these values do not necessarily have to be equal, which means that a Bézier segment can contain more than one width segment. The calculation of the line segments is based on a least square error. When the calculated error is larger than a certain value, a new segment is created. The \(W_1\) and \(W_2\) values of the new segment are equal to the \(W_2\) value of the last segment, which provides a smooth transition of the line width; otherwise the \(W_2\) value of the current line segment is set equal to the width of the last data point.
Editing

Currently, two major editing tools are implemented: local modifications and transformations.

Local Modifications

Sometimes, the user is not entirely satisfied with the sketch that is made. Instead of having to redraw the sketch, local modifications can be made. Since we make use of cubic Bézier splines, the problem of modifying a sketch can be reduced to moving the control points of the segments. However, most people are not familiar with cubic Bézier splines and find it hard to get the desired result. Therefore, our tool lets the user pull and push against the curve. The control points are transformed transparently in such a manner that the modification of the sketch mimics the user’s movement, thus allowing to intuitively redraw part of the sketch. We do this by sketching the modification in the neighborhood of the curve: the curve is pulled towards the pointer. This process consists of three steps and is repeatedly executed during the modification stage.

Selecting a Point on the Curve. To select the point nearest to the pen position we first need to determine the nearest Bézier segment. Since our tool makes use of OpenGL for rendering, the OpenGL picking functionality can be used (Woo et al. 1999). Next, the selected point on the Bézier spline is determined by calculating the above-mentioned t-value. This t-value is determined so that the distance between the PHANToM position and the corresponding point is as small as possible.

The distance between the PHANToM position \((x, y, z)\) and the spline is given by:

\[
g(t) = (x - f_x(t))^2 + (y - f_y(t))^2 + (z - f_z(t))^2
\] (4)

The desired t-value is found by solving the following equation for \(t\) (Vansichem, Wauters, & van Reeth 2001).

\[
\frac{\partial g(t)}{\partial t} = 0
\] (5)

Modifying the Curve. Next, a vector \(\vec{V}\) is defined:

\[
\vec{V} = (x, y, z) - (f_x(t), f_y(t), f_z(t))
\] (6)

To adjust the Bézier segment, the vector \(\vec{V}\) needs to be distributed over its control points. The influence of \(\vec{V}\) on each of the control points is determined by the basis functions for a cubic Bézier spline. So the new control points \(B'_1, B'_2, B'_3\) and \(B'_4\) are given by:

\[
\begin{align*}
B'_1 &= B_1 + (1 - t)^3 \vec{V} \\
B'_2 &= B_2 + 3t(1-t)^2 \vec{V} \\
B'_3 &= B_3 + 3t^2(1-t) \vec{V} \\
B'_4 &= B_4 + t \vec{V}
\end{align*}
\] (7)

In order to keep the smoothness at the transition from one segment to another, the control points from the previous and next segment will also be moved. We can distinguish three different cases for the values of \(t\):

1. \(t \approx 0\): Both the control points \(B_1\) and \(B_2\) of the selected segment as well as \(B_3\) and \(B_4\) of the previous segment will be moved over the distance \(\vec{V}\).

2. \(t \approx 1\): Both the control points \(B_3\) and \(B_4\) of the selected segment as well as \(B_1\) and \(B_2\) of the next segment will be moved over the distance \(\vec{V}\).

3. \(t \in [0, 1]\): \(B_2\) and \(B_3\) of the selected segment are moved over \(\frac{\vec{V}}{3(1-t)}\). The smoothness is preserved by rotating \(B_3\) of the previous segment around \(B_1\) of the selected segment and by rotating \(B_2\) of the next segment around \(B_4\) of the selected segment.

Haptic Feedback. When modifying a sketch, a force is fed back to the user which resists the movement. This force counterbalances the movement of the curve: the pointer is drawn to the curve with a force \((\vec{F})\) proportional to the force with which the curve is pulled to the pointer:

\[
\vec{F} = -l(\vec{V}).
\] (8)

The function \(l\) scales the magnitude of \(\vec{V}\) in such a manner that equation 9 is true.

\[
0.2N \leq \|\vec{F}\| \leq 1N
\]

\[
\|\vec{V}_1\| < \|\vec{V}\| \Rightarrow \|l(\vec{V}_1)\| < \|l(\vec{V})\|
\] (9)

This force reduces errors by making large movements harder to perform. On the other hand the forces that are generated are never so big that they hinder (or fatigue) the user.

Transformations

Most bitmap editors provide a selection tool and tools to transform selections. Likewise, our tool provides a lasso selection tool. Unlike bitmap editors, the tool doesn’t select the pixels within the selection area, but the control points within the selection area. This allows for a more efficient manipulation of the part of the sketch in which the user is interested.

A number of tools are implemented which transform the segments of which one or more control points are selected. The selected area can either be translated, rotated or scaled down. Because these tools work on the cubic Bézier splines and not on individual pixels, the connectivity between the curves is kept.

Again, force feedback can help when performing these editing tasks: by defining different effects to counteract the modifications, the user is guided during the manipulation task. The force that counteracts the transformations is dependent on the curves that partially belong to the selection. More exactly it is dependent on the first control points \((B_1\) or \(B_4)) along the curves who are not part of the selection. This way the force increases with the amount of curves that connect the selected with the non-selected part of the sketch. This makes it harder to move a selection that has a tight connection with its surroundings.
Translation. The force is a scaled sum of the translations of the mentioned control points:

\[ \begin{align*}
\vec{V}_1 &= (x, y, z) - B_1 \\
\vec{V}_4 &= (x, y, z) - B_4 \\
\vec{F} &= -l(\vec{V}_1 + \vec{V}_4)
\end{align*} \] (10)

Rotation. The size of the force is a scaled sum of the alleged translation of the mentioned control points. The direction is perpendicular to the vector from the center of the rotation to the position of the pen. The calculation of the counteracting force is depending on the type of transformation, as depicted in figures 3 and 4, which depict the rotation force at two moments during the interaction (rotating the head of a cat).

Scale. The force is a scaled sum of the alleged scale of the mentioned control points. These calculations are analogous to the calculations in the translation case.

**Additional Functionality**

Next to creating a curve and modifying its position, we can also define a wide range of additional tools, which can also be implemented without exposing the mathematical structures to the user. In this paragraph we will shortly describe some of these tools.

**Eraser**

Erasing a part of a sketch can be done by selecting the nearest point to the cursor with each move of the eraser. Subdividing the Bézier segment and width segment at this point allows us to delete the part of the segment traversed by the eraser without any changes to the rest of the sketch.

The acting force works the same as with the creation of a curve, only with a different scale according to the difference in material (pencil versus eraser). This effect is achieved by altering the resistance of the haptic plane. A pencil moves more easily over a piece of paper than an eraser. An increase in friction mimics this effect and decreases the number of errors that are made because the user has more difficulties to move the pointer of the friction is larger.

**Connect Curves**

An additional property of the drawing tools is the possibility to automatically connect the start or end points of the newly drawn curve to neighboring curves. With this addition it is also possible to create closed curves.

The end point of the curve is snapped towards the begin point if the pointer (thus the end point) comes in the vicinity of the begin point. Likewise, the user feels an attracting force towards the begin point:

\[ \begin{align*}
\vec{V} &= P_0 - (x, y, z) \\
\|\vec{V}\| < M &\Rightarrow \vec{F} = l(\vec{V})
\end{align*} \] (11)

The begin point is indicated by \( P_0 \), the pointer position by \((x, y, z)\) and \(l\) is the function that was discussed in the paragraph about editing. The parameter \( M \) defines a circle in which the effect is felt. We can hereby control if the user should feel the force before the curve is snapped to the begin point.

This force also allows us to turn of the snapping of the sketch. It is possible that the user wants to sketch near the begin point, but does not want the sketch to snap. If only the force is active, but not the sketch snapping, the user can avoid this snapping effect by simply resisting the force.
Change Curve Width

Previously, a tool for correcting the position of the curve was described. It is also possible to modify the width of the curve. This is done again by selecting the nearest point to the cursor on the curve. But instead of changing a Bézier segment, the width segment will be modified by increasing or decreasing the width at its start and/or end point. It is also possible to subdivide the line segment when more level of detail is needed.

The size of the width modification is dependent on the pressure in the z direction exercised by the user. The maximum width is limited because the pressure of the user against the plane is counteracted by a spring-damper system.

Future Work

Using force feedback, it is possible to mimic different types of drawing surfaces, like paper or a blackboard. Although, the research into this kind of haptic “textures” is still very recent (McGee, Gray, & Brewster 2001), it is already incorporated into e-Touch (Novint 2001), a device-independent haptic API.

These haptic textures can be combined with visual textures (e.g. a crayon-like texture) in order to get a truly “look and feel” of different kinds of physical surfaces.

Conclusions

This paper discussed a tool for intuitively drawing sketches. The tools uses an mathematical model for the sketch, without the user having to know this representation. This setup provides the user with a powerful set of editing tools.

Special attention was paid to the use of force feedback. This allows the user to efficiently create sketches and to make corrections without have to redraw the entire sketch.

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References