ProjE: Embedding Projection for Knowledge Graph Completion

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Abstract

With the large volume of new information created every day, determining the validity of information in a knowledge graph and filling in its missing parts are crucial tasks for many researchers and practitioners. To address this challenge, a number of knowledge graph completion methods have been developed using low-dimensional graph embeddings. Although researchers continue to improve these models using an increasing complexity feature space, we show that simple changes in the architecture of the underlying model can outperform state-of-the-art models without the need for complex feature engineering. In this work, we present a shared variable neural network model called ProjE that fills-in missing information in a knowledge graph by learning joint embeddings of the knowledge graph’s entities and edges, and through subtle, but important, changes to the standard loss function. In doing so, ProjE has a parameter size that is smaller than 11 out of 15 existing methods while performing 37% better than the current-best method on standard datasets. We also show, via a new fact checking task, that ProjE is capable of accurately determining the veracity of many declarative statements.

Introduction

Knowledge Graphs (KGs) have become a crucial resource for many tasks in machine learning, data mining, and artificial intelligence applications including question answering (Unger et al. 2012), entity disambiguation (Cucerzan 2007), named entity linking (Hachey et al. 2013), fact checking (Unger et al. 2012), entity disambiguation (Cucerzan 2015), incorporate a multilayer neural network solution into the existing models. Unfortunately, due to their extremely large parameter size, these models either (i) do not scale well or (2) consider only a single relationship at a time (Garcia-Duran, Bordes, and Usunier 2015) in order to predict the existence of \( \langle h, r, ? \rangle \) in the KG.

The KGC task can be divided into two non-mutually exclusive sub-tasks: (i) entity prediction and (ii) relationship prediction. The entity prediction task takes a partial triple \( \langle h, r, ? \rangle \) as input and produces a ranked list of candidate entities as output:

**Definition 1.** (Entity Ranking Problem) Given a Knowledge Graph \( G = \{ E, R \} \) and an input triple \( \langle h, r, ? \rangle \), the entity ranking problem attempts to find the optimal ordered list such that \( \forall e_i \in \{ E_- \} \) and \( e_i \rightarrow e_i \), where \( E_+ = \{ e \in \{ e_1, e_2, \ldots, e_l \} | \langle h, r, e \rangle \in G \} \) and \( E_- = \{ e \in \{ e_{l+1}, e_{l+2}, \ldots, e_{|E|} \} | \langle h, r, e \rangle \notin G \} \).

Distinguishing between head and tail-entities is usually arbitrary, so we can easily substitute \( \langle h, r, ? \rangle \) for \( \langle ?, r, t \rangle \). The relationship prediction task aims to find a ranked list of relationships that connect a head-entity with a tail-entity, i.e., \( \langle h, ?, t \rangle \). When discussing the details of the present work, we focus specifically on the entity prediction task; however, it is straightforward to adapt the methodology to the relationship prediction task by changing the input.

A number of KGC algorithms have been developed in recent years, and the most successful models all have one thing in common: they use low-dimensional embedding vectors to represent entities and relationships. Many embedding models, e.g., Unstructured (Bordes et al. 2012), TransE (Bordes et al. 2013), TransH (Wang et al. 2014), and TransR (Lin et al. 2015), use a margin-based pairwise ranking loss function, which measures the score of each possible result as the \( L_n \)-distance between \( h + r \) and \( t \). In these models the loss functions are all the same, so models differ in how they transform the entity embeddings \( h \) and \( t \) with respect to the relationship embeddings \( r \). Instead of simply adding \( h + r \), more expressive combination operators are learned by Knowledge Vault (Dong et al. 2014) and HolE (Nickel, Rosasco, and Tomaso 2016) in order to predict the existence of \( \langle h, r, t \rangle \) in the KG.

Other models, such as the Neural Tensor Network (NTN) (Socher et al. 2013) and the Compositional Vector Space Model (CVSM) (Neelakantan, Roth, and McCallum 2015), incorporate a multilayer neural network solution into the existing models. Unfortunately, due to their extremely large parameter size, these models either (i) do not scale well or (2) consider only a single relationship at a time (Garcia-Duran, Bordes, and Usunier 2015) thereby limiting their usefulness on large, real-world KGs.
Despite their large model size, the aforementioned methods only use singleton triples, i.e., length-1 paths in the KG. PTransE (Lin, Liu, and Sun 2015) and RTransE (García-Durán, Bordes, and Usunier 2015) employ extended path information from 2 and 3-hop trails over the knowledge graph. These extended models achieve excellent performance due to the richness of the input data; unfortunately, their model size grows exponentially as the path-length increases, which further exacerbates the scalability issues associated with the already high number of parameters of the underlying-models.

Another curious finding is that some of the existing models are not self-contained models, i.e., they require pre-trained KG embeddings (RTransE, CVSM), pre-selected paths (PTransE, RTransE), or pre-computed content embeddings of each node (DKRL (Xie et al. 2016)) before their model training can even begin. TransR and TransH are self-contained models, but their experiments only report results using pre-trained TransE embeddings as input.

With these considerations in mind, in the present work we reframe some of the basic decisions made by previous models to create a projection embedding model (ProjE) for KGC. ProjE has four parts that distinguish it from the related work: 1. Instead of measuring the distance between input triple \((h, r, ?)\) and entity candidates on a unified or a relationship-specific plane, we choose to project the entity candidates onto a target vector representing the input data. 2. Unlike existing models that use transformation matrices, we combine the embedding vectors representing the input data into a target vector using a learnable combination operator. This avoids the addition of a large number of transformation matrices by reusing the entity-embeddings. 3. Rather than optimizing the margin-based pairwise ranking loss, we optimize a ranking loss of the list of candidate-entities (or relationships) collectively. We further use candidate sampling to handle very large data sets. 4. Unlike many of the related models that require pre-trained data from prerequisite models or explore expensive multi-hop paths through the knowledge graph, ProjE is a self-contained model over length-1 edges.

**Related Work**

A variety of low-dimensional representation-based methods have been developed to work on the KGC task. These methods usually learn continuous, low-dimensional vector representations (i.e., embeddings) for entities \(W^E\) and relationships \(W^R\) by minimizing a margin-based pairwise ranking loss (Lin, Liu, and Sun 2015).

The most widely used embedding model in this category is TransE (Bordes et al. 2013), which views relationships as translations from a head entity to a tail entity on the same low-dimensional plane. The energy function of TransE is defined as

\[
E(h, r, t) = || h + r - t ||_{L_1},
\]

which measures the \(L_1\)-distance between a translated head entity \(h+r\) and some tail entity \(t\). The Unstructured model (Bordes et al. 2012) is a special case of TransE where \(r = 0\) for all relationships.

Based on the initial idea of treating two entities as a translation of one another (via their relationship) in the same embedding plane, several models have been introduced to improve the initial TransE model. The newest contributions in this line of work focus primarily on the changes in how the embedding planes are computed and/or how the embeddings are combined. For example, the entity translations in TransH (Wang et al. 2014) are computed on a hyperplane that is perpendicular to the relationship embedding. In TransR (Lin et al. 2015) the entities and relationships are embedded on separate planes and then the entity-vectors are translated to the relationship’s plane. Structured Embedding (SE) (Bordes et al. 2011) creates two translation matrices for each relationship and applies them to head and tail entities separately. Knowledge Vault (Dong et al. 2014) and HolE (Nickel, Rosasco, and Tomaso 2016), on the other hand, focus on learning a new combination operator instead of simply adding two entity embeddings element-wise.

The aforementioned models are all geared toward link prediction in KGs, and they all minimize a margin-based pairwise ranking loss function \(\mathcal{L}\) over the training data \(\mathbf{S}\):

\[
\mathcal{L}(\mathbf{S}) = \sum_{(h, r, t) \in \mathbf{S}} [\gamma + E(h, r, t) - E(h', r', t')],
\]

where \(E(h, r, t)\) is the energy function of each model, \(\gamma\) is the margin, and \((h', r', t')\) denotes some “corrupted” triple which does not exist in \(\mathbf{S}\). Unlike aforementioned models that focus on different \(E(h, r, t)\), TransA (Jia et al. 2016) introduces an adaptive local margin approach that determines \(\gamma\) by a closed set of entity candidates. Other similar models include RESCAL (Nickel, Tresp, and Kriegel 2011), Semantic Matching Energy (SME) (Bordes et al. 2012), and the Latent Factor Model (LFM) (Jenatton et al. 2012).

The Neural Tensor Network (NTN) model (Socher et al. 2013) is an exception to the basic energy function in Eq. 1. Instead, NTN uses an energy function

\[
E(h, r, t) = u_x^T f(h^T W_r t + W_{rh} h + W_{rt} t + b_r),
\]

where \(u_x, W_r, W_{rh},\) and \(W_{rt}\) are all relationship-specific variables. As a result, the number of parameters in NTN is significantly larger than other methods. This makes NTN unsuitable for networks with even a moderate number of relationships.

So far, the related models have only considered triples that contain a single relationship. More complex models have been introduced to leverage path and content information in KGs. For instance, the Compositional Vector Space Model (CVSM) (Neelakantan, Roth, and McCallum 2015) compiles a sequence of relationship embeddings into a single path embedding using a Recurrent Neural Network (RNN). However, this has two disadvantages: (i) CVSM needs pre-trained relationship embeddings as input, and (ii) each CVSM is specifically trained for only a single relationship type. This makes CVSM perform well in specific tasks, but unsuitable for generalized entity and relationship prediction tasks. RTransE (García-Durán, Bordes, and Usunier 2015) solves the relationship-specific problem in CVSM by using entity and relationship embeddings learned from TransE.
Table 1: Parameter size and prerequisites of KGC models in increasing order. ProjE, ranked 5th, is highlighted. \(n_e, n_r, n_w, k\) are the number of entities, relationships, words, and embedding size in the KG respectively. \(z\) is the hidden layer size. \(q_i\) represents the number of RNN parameters in RTransE; this value is not specified, but should be \(5k^2\) if a normal LSTM is used.

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameters</th>
<th>Prerequisites</th>
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<tr>
<td>Unstructured</td>
<td>(n_e)</td>
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<tr>
<td>TransE</td>
<td>(n_e + n_e)</td>
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<td>HoIE</td>
<td>(n_e + n_e)</td>
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<td>PTransE</td>
<td>(n_e + n_e)</td>
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<td>ProjE</td>
<td>(n_e + n_e + n_{e/5k})</td>
<td>PCRA</td>
</tr>
<tr>
<td>CVSM</td>
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<td>Word2vec</td>
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<tr>
<td>SME (linear)</td>
<td>(n_e + n_e + 4k^2)</td>
<td>TransE, PCRW</td>
</tr>
<tr>
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<tr>
<td>LFM</td>
<td>(n_e + n_e + 10k^2)</td>
<td>-</td>
</tr>
<tr>
<td>SME (bilinear)</td>
<td>(n_e + n_e + k^2)</td>
<td>-</td>
</tr>
<tr>
<td>TransH</td>
<td>(n_e + 2n_e)</td>
<td>-</td>
</tr>
<tr>
<td>RESCAL</td>
<td>(n_e + n_e)</td>
<td>-</td>
</tr>
<tr>
<td>SE</td>
<td>(n_e + 2n_e)</td>
<td>-</td>
</tr>
<tr>
<td>TransR</td>
<td>(n_e + n_e + k^2)</td>
<td>-</td>
</tr>
<tr>
<td>DKRL</td>
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<td>TransE, Word2vec</td>
</tr>
<tr>
<td>NTN</td>
<td>(n_e + n_e + 2k + 2z)</td>
<td>-</td>
</tr>
</tbody>
</table>

However, it is hard to compare RTransE with existing methods because it requires unambiguous, pre-selected paths as inputs called quadruples \(\langle h, r_1, r_2, t\rangle\) further complicating the model. DKRL, like NTN, uses word embeddings of entity-content in addition to multi-hop paths, but relies on the machinery of a Convolution Neural Network (CNN) to learn entity and relationship embeddings.

PTransE (Lin, Liu, and Sun 2015) is another path-based method that uses path information in its energy function. Simply put, PTransE doubles the number of edges in the KG by creating reverse relationships for every existing relationship in the KG. Then PTransE uses PCRA (Zhou et al. 2007) to select input paths within a given length constraint.

Table 1 shows a breakdown of the parameter complexity of each model. As is typical, we find that more complex models achieve better prediction accuracy, but are also more difficult to train and have trouble scaling. The proposed method, ProjE, has a number of parameters that is smaller than 11 out of 15 methods and does not require any prerequisite training.

### Methodology

The present work views the KGC problem as a ranking task and optimizes the collective scores of the list of candidate entities. Because we want to optimize the ordering of candidate entities collectively, we need to project the candidate entities onto the same embedding vector. For this task we learn a combination operator that creates a target vector from the input data. Then, the candidate entities are each projected onto the same target vector thereby revealing the candidate’s similarity score as a scalar.

In this section we describe the ProjE architecture, followed by two proposed variants, their loss functions, and our choice of candidate sampling method. In the experiments section we demonstrate that ProjE outperforms all existing methods despite having a relatively small parameter space. A detailed algorithm description can be found in the Supplementary Material.

### Model Architecture

The main insight in the development of ProjE is as follows: given two input embeddings, we view the prediction task as ranking problem where the top-ranked candidates are the correct entities. To generate this ordered list, we project each of the candidates onto a target vector defined by two input embeddings through a combination operator.

Existing models, such as Knowledge Vault, HolE, and NTN, define specific matrix combination operators that combine entities and/or relationships. In common practice, these matrices are expected to be sparse. Because we believe it is unnecessary to have interactions among different feature dimensions at this early stage, we constraint our matrices to be diagonal, which are inherently sparse. The combination operator is therefore defined as

\[
\mathbf{e} \oplus \mathbf{r} = \mathbf{D}_e \mathbf{e} + \mathbf{D}_r \mathbf{r} + \mathbf{b}_e,
\]

where \(\mathbf{D}_e\) and \(\mathbf{D}_r\) are \(k \times k\) diagonal matrices which serve as global entity and relationship weights respectively, and \(\mathbf{b}_e \in \mathbb{R}^k\) is the combination bias.

Using this combination operator, we can define the embedding projection function as

\[
h(\mathbf{e}, \mathbf{r}) = g(\mathbf{W}^c f(\mathbf{e} \oplus \mathbf{r}) + b_p),
\]

where \(f\) and \(g\) are activation functions that we define later, \(\mathbf{W}^c \in \mathbb{R}^{s \times k}\) is the candidate-entity matrix, \(b_p\) is the projection bias, and \(s\) is the number of candidate-entities. \(h(\mathbf{e}, \mathbf{r})\) represents the ranking score vector, where each element represents the similarity between some candidate entity in \(\mathbf{W}^c\) and the combined input embedding \(\mathbf{e} \oplus \mathbf{r}\).

Although \(s\) is relatively large, due to the use of shared variables, \(\mathbf{W}^c\) is the candidate-entity matrix that contains \(s\) rows that exist in the entity embedding matrix \(\mathbf{W}^E\). Simply put, \(\mathbf{W}^c\) does not introduce any new variables into the model. Therefore, compared to simple models like TransE, ProjE only increases the number of parameters by \(5k^2 + 1\), where 1, \(4k\), and \(k\) are introduced as the projection bias, combination weights, and combination bias respectively. Later we show that by changing different activation functions, ProjE can be either a pointwise ranking model or a listwise ranking model.

ProjE can be viewed as a neural network with a combination layer and a projection (i.e., output) layer. Figure 1 illustrates this architecture by way of an example. Given a tail entity Illinois and a relationship CityOf, our task is to calculate the scores of each head entity. The blue nodes are row vectors from the entity embedding matrix \(\mathbf{W}^E\), and the green nodes are row vectors from the relationship embedding matrix \(\mathbf{W}^R\); the orange nodes are the combination operators as diagonal matrices. For clarity we only illustrate two candidates in Fig. 1, however \(\mathbf{W}^c\) may contain an arbitrary number of candidate-entities.

The next step is to define the loss functions used in ProjE.
As defined in Defn. 1, we view the KGC problem as a rank-wise method when deployed. Based on the architecture we described in previous section, we propose two methods: 1) ProjE_pointwise, and 2) ProjE_listwise through the use of different activation functions for $g(\cdot)$ and $f(\cdot)$ in Eq. 5.

First we describe the ProjE_pointwise ranking method. Because the relative order inside each entity set does not affect the prediction power, we can create a binary label vector in which all entities in $E_i$ have a score of 0, and all entities in $E_j$ have a score of 1. Because we maximize the likelihood between the ranking score vector $h(e, r)$ and the binary label vector, it is intuitive to view this task as a multiclass classification problem. Therefore, the loss function of ProjE_pointwise can be defined in a familiar way:

$$
\mathcal{L}(e, r, y) = - \sum_{i \in \{y_i = 1\}} \log(h(e, r)_i) - \sum_m E_{j \sim P_y} \log(1 - h(e, r)_j),
$$

where $e$ and $r$ are the input embedding vectors of a training instance in $S$, $y \in \mathbb{R}^n$ is a binary label vector where $y_i = 1$ means candidate $i$ represents a positive label, $m$ is the number of negative samples drawn from a negative candidate distribution $E_{j \sim P_y}$ (described in next section). Because we view ProjE_pointwise as a multiclass classification problem, we use the sigmoid and tanh activation functions as our choice for $g(\cdot)$ and $f(\cdot)$ respectively. When deployed, the ranking score of the $i^{th}$ candidate-entity is:

$$
h(e, r)_i = \text{sigmoid}(W_{[i,:]}^c \cdot \text{tanh}(e \oplus r) + b_p),
$$

where $W_{[i,:]}^c$ represents $i^{th}$ candidate in the candidate-entity matrix.

Recently, softmax regression loss has achieved good results in multi-label image annotation tasks (Guillaumin et al. 2009; Gong et al. 2013). This is because multi-label image annotation, as well as many other classification tasks, should consider their predicted scores collectively. Inspired by this way of thinking, we employ the softmax activation function in order to classify candidate-entities collectively, i.e., using a listwise method. In this case we define the loss function of ProjE_listwise as:

$$
\mathcal{L}(e, r, y) = - \sum_{i} \frac{1}{\sum_{j} \mathbb{1}(y_i = 1)} \log(h(e, r)_i),
$$

where the target probability (i.e., the target score) of a positive candidate is 1 / (total number of positive candidates of the input instance). Similar to Eq. 7, we replace $g(\cdot)$ and $f(\cdot)$ as softmax and tanh respectively, which can be written equivalently as:

$$
h(e, r)_i = \frac{\exp(W_{[i,:]}^c \cdot \text{tanh}(e \oplus r) + b_p)}{\sum_j \exp(W_{[j,:]}^c \cdot \text{tanh}(e \oplus r) + b_p)}. 
$$

Later, we perform a comprehensive set of experiments that compare ProjE with more than a dozen related models and discuss the proposed ProjE_pointwise and ProjE_listwise variants in depth.

Candidate Sampling

Although ProjE limits the number of additional parameters, the projection operation may be costly due to the large number of candidate-entities (i.e., the number of rows in $W^c$). If we reduce the number of candidate-entities in the training phrase, we could create a smaller working set that only contains a subset of the embedding matrix $W^E$. With this in mind, we use candidate sampling to reduce the number of candidate-entities. Candidate sampling is not a new problem; many recent works have addressed this problem in interesting ways (Jean et al. 2015; Mikolov et al. 2013; Gutmann and Hyvärinen 2010). We experimented with many choices, and found that the negative sampling used in Word2Vec (Mikolov et al. 2013) resulted the best performance.

For a given entity $e$, relationship $r$, and a binary label vector $y$, we compute the projection with all of the positive candidates and only a sampled subset of negative candidates from $P_y$ following the convention of Word2Vec. For simplicity, $P_y$ can be replaced by a $(0,1)$ binomial distribution.
We evaluate the ProjE model with entity prediction and regularizer weight $\alpha$, dropout probability $p_d$, and success probability for negative candidate sampling $p_y$. We set $lr = 0.01$, $b = 200$, $\alpha = 1e^{-5}$, and $p_d = 0.5$ for both tasks, $k = 200$, $p_y = 0.5$ for the entity prediction task and $k = 100$, $p_y = 0.75$ for the relationship prediction task.

For all tasks, ProjE was trained for at most 100 iterations, and all parameters were initialized from a uniform distribution $U[-0.05, 0.05]$ as suggested by TransE (Bordes et al. 2013). ProjE can also be initialized with pre-trained embeddings.

### Entity and Relationship Prediction

We evaluated ProjE’s performance on entity and relationship prediction tasks using the FB15K dataset following the experiment settings in TransE (Bordes et al. 2013) and PTransE (Lin, Liu, and Sun 2015). For entity prediction, we aim to predict a missing $h$ (or $t$) for a given triple $(h, r, t)$ by ranking all of the entities in the KG. To create a test set we replaced the head or tail-entity with all entities in the KG, and rank these replacement entities in descending order. For relationship prediction, we replaced the relationship of each test triple with all relationships in the KG, and rank these replacement relationships in descending order.

Following convention, we use mean rank and HITS@k as evaluation metrics. Mean rank measures the average rank of correct entities/relationships, HITS@k measures if correct entities/relationships appear within the top-$k$ elements. The filtered mean rank and filtered HITS@k ignore all other true entities/relationships in the result and only look at the target entity/relationship. For example, if the target relationship between Springfield, Illinois, is locatedIn, and the top-2 ranked relationships are capitalOf and locatedIn, then the raw mean rank and HITS@1 of this example would be 2 and 0 respectively, but the filtered mean rank and filtered HITS@1 ignore the correct capitalOf relationship in the results set.

In addition to ProjE_pointwise and ProjE_listwise, we also evaluate ProjE_wlistwise, which is a slight variation of ProjE_listwise that incorporates instance-level weights (\$\Sigma_i f(y_i = 1)\$) to increase the importance of N-to-N and N-to-1 (1-to-N) relationships.

Table 2 and Tab. 3 show that the three ProjE variants outperform existing methods in most cases. Table 3 contains fewer models than Tab. 2 because many models do not per-
form the relationship prediction task. We also adapt the pointwise and listwise ranking methods to TransE using the same hyperparameter settings, but the performance does not improve significantly and is not shown here. This indicates that the pointwise and listwise ranking methods are not merely simple tricks that can be added to any model to improve performance.

Surprisingly, although softmax is usually used in mutually exclusive multi-class classification problems and sigmoid is a more natural choice for non-exclusive cases like the KGC task, we find that ProjE_listwise and ProjE_wlistwise perform better than ProjE_pointwise in most cases. This is because KGC is a special ranking task, where a good model ought to have the following properties: 1) the score of all positive candidates should be maximized and the score of all negative candidates should be minimized, and 2) the number of positive candidates that are ranked above negative candidates should be maximized. By maximizing the similarity between the ranking score vector and the binary label vector, ProjE_pointwise meets the first property but fails to meet the second, i.e., ProjE_pointwise does not addresses the ranking order of all candidates collectively, because sigmoid is applied to each candidate individually. On the other hand, ProjE_listwise and ProjE_wlistwise successfully addresses both properties by maximizing the similarity between the binary label vector and the ranking score vector, which is an exponential-normalized ranking score vector that imposes an explicit ordering to the candidate-entities collectively.

In the Supplementary Material we also examine the stability of the proposed ProjE model and demonstrate that the performance of ProjE increases steadily and smoothly during training.

**Fact Checking**

Unlike the entity prediction and relationship prediction tasks that predict randomly sampled triples, we employ a new fact checking task that tests the predictive power of various models on real world questions. We view the fact checking task as a type of link prediction problem because a fact statement \( \langle h, r, t \rangle \) can be naturally considered as an edge in a KG.

We use ProjE_wlistwise with a small change: rather than using entity embeddings directly, the input vector of ProjE consists of the predicate paths between the two entities (Shi and Weninger 2016). We learn the entity-embeddings by adding an input layer that converts input predicate paths into the entity-embedding.

We employ the experimental setup and question set from Shi and Weninger (2016) on the DBpedia and SemMedDB data sets. Specifically, we remove all edges having the same label as the input relationship \( r \) and perform fact checking on the modified KG by predicting the existence of \( r \) on hundreds of variations of 7 types of questions. For example, the CapitalOf question checks various claims of the capitals of US states. In this case, we check if each of the 5 most populous cities within each state is its capital. This results in about \( 5 \times 5 = 250 \) checked facts with an 20/80 positive to negative label ratio. The odds that some fact statement is true is equivalent to the odds that the fact’s triple is missing from the KG (rather than purposefully omitted, i.e., a true negative). Results in Tab. 4 show that ProjE outperforms existing fact checking and link prediction models (Adamic and Adar 2003; Ciampaniglia et al. 2015; Jeh and Widom 2002; Galárraga et al. 2013; Haveliwala 2002; Lao and Cohen 2010) in all but one question type.

**Conclusions and Future Work**

To recap, the contributions of the present work are as follows: 1) we view the KGC task as a ranking problem and project candidate-entities onto a vector representing a combined embedding of the known parts of an input triple and order the ranking vector score in descending order; 2) we show that by optimizing the ranking score vector collectively using the listwise ProjE variation, we can significantly improve prediction performance; 3) ProjE uses only directly connected, length-1 paths during training, and has a relatively simple 2-layer structure, yet outperforms complex models that have a richer parameter or feature set; and 4) unlike other models (e.g., CVSM, RTransE, DKRL), the present work does not require any pre-trained embeddings and has many fewer parameters than related models. We finally show that ProjE can outperform existing methods on fact checking tasks.

For future work, we will adapt more complicated neural network models such RNN and CNN with the embedding projection model presented here. It is also possible to incorporate rich feature sets from length-2 and length-3 paths, but these would necessarily add additional complexity. Instead, we plan to use information from complex paths in the KG to clearly summarize the many complicated ways in which entities are connected.

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<th>Algorithm</th>
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<th>SemMedDB</th>
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<tr>
<td></td>
<td>CapitalOf</td>
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References


Mikolov, T.; Sutskever, I.; Chen, K.; Corrado, G. S.; and Dean, J. 2013. Distributed representations of words and phrases and their compositionality. In *NIPS*.


